

## Exeter Math problem set #3

1. Draw the following segments. What do they have in common? from  $(3, -1)$  to  $(10, 3)$ ; from  $(1.3, 0.8)$  to  $(8.3, 4.8)$ ; from  $(\pi, \sqrt{2})$  to  $(7 + \pi, 4 + \sqrt{2})$ .

The *directed segments* have the same length and the same direction. Each represents the *vector*  $[7, 4]$ . The components of the vector are the numbers 7 and 4.

2. (Continuation)

(a) Find another example of a directed segment that represents this vector. The initial point of your segment is called the *tail* of the vector, and the final point is called the *head*.

(b) Which of the following directed segments represents  $[7, 4]$ ?

i) from  $(-2, -3)$  to  $(5, -1)$

ii) from  $(-3, -2)$  to  $(11, 6)$

iii) from  $(10, 5)$  to  $(3, 1)$

iv) from  $(-7, -4)$  to  $(0, 0)$

3. Given the vector  $[-5, 12]$ , find the following vectors:

(a) same direction, twice as long

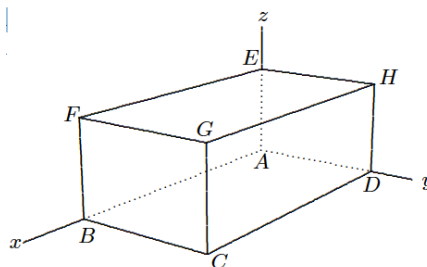
(b) same direction, length 1

(c) opposite direction, length 10

(d) opposite direction, length c

4. The diagram shows a rectangular box named ABCDEFGH. Notice that  $A = (0, 0, 0)$ , and that B, D, and E are on the coordinate axes. Given that  $G = (6, 3, 2)$ , find

(a) coordinates for the other six vertices;



(b) the lengths AH, AC, AF, and AG.

5. The edges of a rectangular solid are parallel to the coordinate axes, and it has the points  $(0, 0, 0)$  and  $(8, 4, 4)$  as diagonally opposite vertices. Make a sketch, labeling each vertex with its coordinates, then find (a) the distance from  $(8, 4, 4)$  to  $(0, 0, 0)$  and (b) the distance from  $(8, 4, 4)$  to the z-axis.